

GCSE Mathematics

Paper 1 43651F Mark scheme

43651F November 2016

Version/Stage: 1.0 Final

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

Μ	Method marks are awarded for a correct method which could lead to a correct answer.
A	Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
В	Marks awarded independent of method.
ft	Follow through marks. Marks awarded for correct working following a mistake in an earlier step.
SC	Special case. Marks awarded for a common misinterpretation which has some mathematical worth.
М dep	A method mark dependent on a previous method mark being awarded.
B dep	A mark that can only be awarded if a previous independent mark has been awarded.
oe	Or equivalent. Accept answers that are equivalent. e.g. accept 0.5 as well as $\frac{1}{2}$
[a, b]	Accept values between a and b inclusive.
[a, b)	Accept values a ≤ value < b
3.14	Accept answers which begin 3.14 e.g. 3.14, 3.142, 3.1416
Q	Marks awarded for quality of written communication
Use of brackets	It is not necessary to see the bracketed work to award the marks.

Examiners should consistently apply the following principles

Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a candidate has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the candidate. In cases where there is no doubt that the answer has come from incorrect working then the candidate should be penalised.

Questions which ask candidates to show working

Instructions on marking will be given but usually marks are not awarded to candidates who show no working.

Questions which do not ask candidates to show working

As a general principle, a correct response is awarded full marks.

Misread or miscopy

Candidates often copy values from a question incorrectly. If the examiner thinks that the candidate has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

Work not replaced

Erased or crossed out work that is still legible should be marked.

Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

Continental notation

Accept a comma used instead of a decimal point (for example, in measurements or currency), provided that it is clear to the examiner that the candidate intended it to be a decimal point.

Paper 1 Foundation Tier

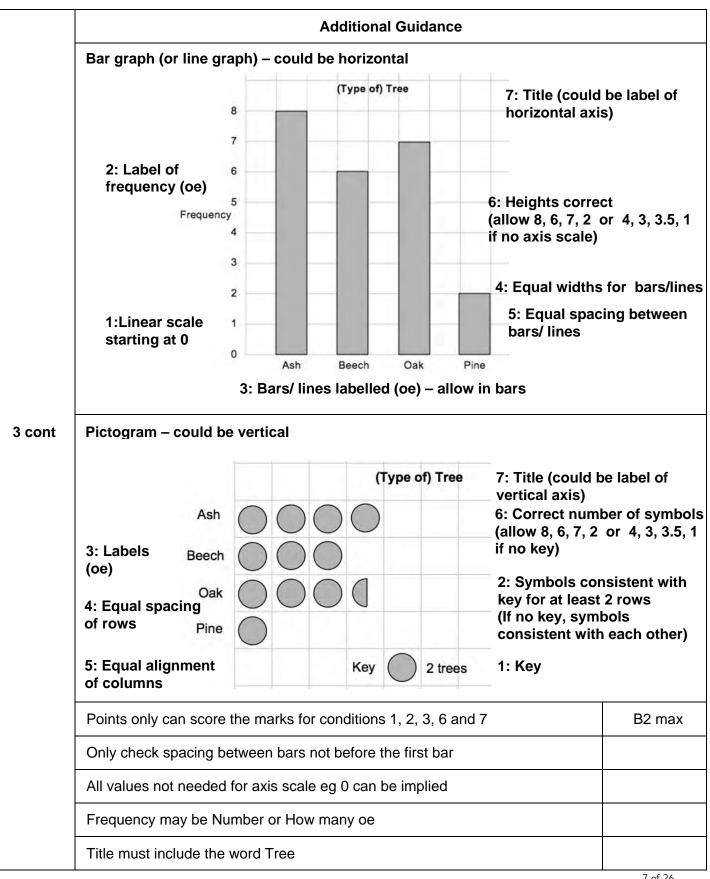
Q	Answer	Mark	Comments
1(a)	72	B1	
	-		
1(b)	36	B1	
			·
1(c)	46	B1	
1(d)	$\frac{2}{5}$	B1	
	•		·
2(a)	436	B1	
2(b)	168	B1	
			·
2(c)	42	B1	Allow 042

Q	Answer	Mark	Comments
	Alternative method 1 Bar chart or	vertical lir	ne graph (could be horizontal)
	Linear scale starting at 0 increasing in 1s or 2s		
	Vertical axis labelled as 'frequency' (or clear reference such as f or freq)		
	Bars/ lines labelled (allow A, B, O, P)		B2 5 or 6 conditions met
	Equal width for bars/ lines	B3	B1 3 or 4 conditions met
	Equal spacing between bars/ lines		
	All heights correct		
3	Title (accept this as a label of horizontal axis)		
	Alternative method 2 Pictogram (v	ertical or	horizontal)
	Pictogram key		
	Consistent symbols for at least 2 rows		
	Labels for trees (allow A, B, O, P)		
	Equal spacing of rows		
	Equal alignment of columns	B3	B2 5 or 6 conditions met B1 3 or 4 conditions met
	Correct number of symbols eg 8, 6, 7, 2 if 1 symbol for 1 tree or 4, 3, 3.5, 1 if 1 symbol for 2 trees		
	Title (accept this as a label of side or bottom 'axis')		

Additional Guidance is on the next page

PMT

Q	Answer	Mark	Comments



Q	Answer	Mark	Comments	
			1	
4(a)	96 or 96.00(p)	B1	96.0 is B0	
4(b)	21	B1		
	37 does not divide (exactly) by 6 or 36 is 6 people and 42 is 7 people or 37 is not in the 6 times table	B1	ое	
	Ad	ditional G	uidance	
	37 is odd / is prime			B1
	It is not (or it should be) even / multiple	es of 6 are	even	B1
	(It is) not in 6 times table / not a multip	B1		
	It ends in a 7			B1
	$6 \times 6 = 36$ and £1	B1		
	$37 \div 6 = 6$ with remainder £1	B1		
	$6 \times 6 = 36, 7 \times 6 = 42$	B1		
4(c)	6, 12, 18, 24, 30, 36, 42			B1
	37 ÷ 6 = 6.1 (Allow 6.1 or 6.2 or 6r1)			B1
	No matter how many times you add 6 it doesn't end in 7			B1
	Only allow 37 doesn't go into 6 if a correct reason is also given eg 37 doesn't go into 6, $37 \div 6 = 6.1$ 37 doesn't go into 6, so it is not in the 6 times table			B1 B1
	Do not allow if an incorrect calculation seen eg $37 \div 6 = 6.5$ so 37 is not a multiple of 6			В0
	£1 too many			В0
	6 × 6 = 36			B0
	37 doesn't go into 6			В0
	Not a whole number			В0
	6, 12, 18, 24, 30, 36 (no further)			B0

Q	Answer	Mark	Comments
	Alternative method 1	-	
	$13 \times 6 \text{ or } 78 \text{ or } 11 \times 6 \text{ or } 66$ or $16 \times 6 \text{ or } 96 \text{ or their } 96 \text{ from (a)}$ or 13 + 11 + 16 or 40	M1	
	their 78 + their 66 + their 96		Must be three products
	or their 40 $ imes$ 6 or 240	M1dep	
	their 240 $ imes$ 0.9		
	or	M1dep	oe
4(d)	their 240 – their 240 \times 0.1		
	216	A1ft	ft their 96 from (a) if used
	Alternative method 2	-	
	13 + 11 + 16 or 40	M1	
	6 × 0.9 or 5.4(0)		
	or	M1	oe
	6 × 0.1 or 0.6(0)		
	their 40 $ imes$ their 5.4		oe
	or	M1dep	dep on M2
	their 40 \times (6 – their 0.6)		
	216	A1	

Q	Answer	Mark	Comments		
	Alternative method 3				
	13 + 11 + 16 or 40	M1			
	their 40 $ imes$ 0.9 or 36				
	or their 40 $ imes$ 0.1 or 4	M1dep	oe		
	their 36 $ imes$ 6				
	or (their 40 – their 4) $ imes$ 6	M1dep	ое		
	216	A1			
	Alternative method 4				
4(d) cont	13×6 or 78 or 11×6 or 66 or 16 \times 6 or 96 or their 96 from (a)	M1			
	their 78 \times 0.9 or 70.2(0) or their 66 \times 0.9 or 59.4(0) or their 96 \times 0.9 or 86.4(0) or their 78 \times 0.1 or 7.8(0) or their 66 \times 0.1 or 6.6(0) or their 96 \times 0.1 or 9.6(0)	M1dep	oe		
	their 70.2 + their 59.4 + their 86.4 or their 78 + their 66 + their 96 – their 7.8 – their 6.6 – their 9.6	M1dep	ое		
	216	A1ft	ft their 96 from (a) if used		

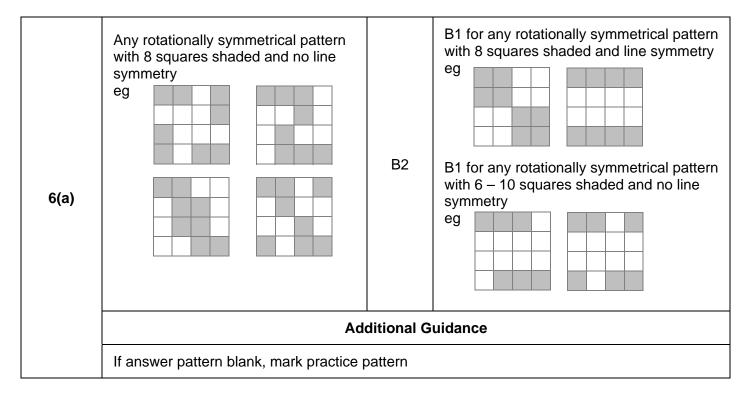
Alternative methods and Additional Guidance continued on the next page

Q	Answer	Mark	Comments			
	Alternative method 5					
	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	M1	oe			
	their 11.7 + their 9.9 + their 14.4 or 36 or their 1.3 + their 1.1 + their 1.6 or 4	M1dep	ое			
4(d) cont	their 36 × 6 or (13 + 11 + 16 – their 4) × 6	M1dep	oe			
	216	A1				
	Additional Guidance					
	Calculation for 10% seen as part of bui not score the method mark for percenta					
	Build-up for percentages must be correct or show full method However allow rounding or truncation eg (for Alt 1) 78 + 66 + 96 = 235 10% = 23 Answer 212					

Q	Answer	Mark	Comments	
	Any two from (3, A), (3, B), (3, E) or (3, F)	B2	Accept coordinates transpos B1 one correct	ed
5(a)	Additional Guidance			
	Accept (3A, 3B), (3E, 3F)			B2

5(b)	No line of 4 (whites) possible	B1	oe		
	Additional Guidance				
	Accept row, path or reference to Connect 4 to imply line				
	Accept maximum of 3 to imply not 4				

5(c)	(4, E)	B1	Allow (E, 4)
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Q	Answer	Mark	Comments		
	$\frac{1}{16} \text{ or } \frac{1}{8} \text{ seen or } \frac{1\frac{1}{2}}{4}$ or diagram divided into 16 squares or 16 seen	M1	oe		
6(b)	$\frac{6}{16}$	A1	oe fraction eg $\frac{3}{8}$		
	Additional Guidance				
	Ignore any incorrect cancelling (except	$\frac{3}{7}$) once of	correct fraction seen		
	0.375 or $\frac{37.5}{100}$			M1 A0	

7(a)	$4 \times 190 \text{ or } 760$ or $4 \times 1.9(0) \text{ or } 7.6(0)$ or 240 or 2.4(0)	M1	oe £240p or £2.40p	
	(£)2.40	Q1	Strand (i)	
	Additional Guidance			
	If building up or down must be correct or show full method			

7(b)	£2, 20p, 20p	B1ft	ft smallest number of coins fo Allow coins or notes used for	
	Additional Guidance			
	Units needed			
	Correct coins in working lines followed by answer 3			B1
	(a) £8.10 (b) (£5) £2 £1 10p or £2 £2 £2 £2 10p			B1ft

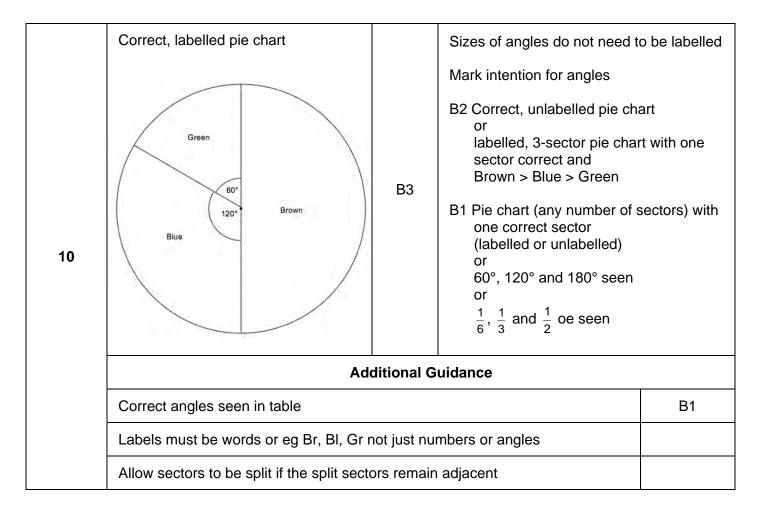
8(a) 8	81	B1	
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8(b)	3.7499	B1	
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Q	Answer	Mark	Comments	
	Alternative method 1			
	(Red) 30 ÷ 3 or 10	M1	oe	
	(Silver) 0.2 $ imes$ 30 or 30 \div 5 or 6	M1	oe	
	(Black) 30 – (their 10 + their 6) or 14	M1dep	dep on at least M1 scored	
	$\frac{14}{30}$ or $\frac{7}{15}$	A1	oe	
	Alternative method 2			
	$(20\% =) \frac{1}{5}$	B1	oe fraction	
9	Correctly converts $\frac{1}{3}$ and their $\frac{1}{5}$ to fractions with a common denominator eg $\frac{5}{15}$ and $\frac{3}{15}$ or $\frac{8}{15}$	M1		
	$1 - (\text{their } \frac{5}{15} + \text{their } \frac{3}{15})$	M1dep		
	<u>7</u> 15	A1	oe	
	Alternative method 3			
	$(\frac{1}{3} =) 0.33(3) \text{ or } 33.(3)\%$	B1	At least 2 sf	
	0.2 + their 0.33 or 0.53(3) or 20% + their 33% or 53.(3)%	M1		
	1 – their 0.53 or 0.47 or 100% – their 53% or 47%	M1dep	At least 2 sf dep on B1M1	
	0.46 or 46.6 %	A1	If exact value seen allow subsequent rounding or truncation	

Additional Guidance is on the next page

Q	Answer	Mark	Comments		
	Additional Guidance				
	red = 10 silver = $0.2 \times (30 - 10) = 4$ 30 - (10 + 4) = 16 $\frac{16}{30}$		M1 M0 M1dep A0		
9 cont	0.3 + 0.2 = 0.5 1 - 0.5 Answer 0.5		B0 M1 M0dep A0		
	0.33 + 0.2 = 0.53 Answer 0.47		B1M1 M1dep A0		
	Ignore any incorrect cancelling or char	e correct answer seen			
	Ignore any probability words once corr	n			



Q	Answer	Mark	Comments	
	21	B1		
	Additional Guidance			
11(a)	Embedded answer only of $21 \div 3 = 7$ or $\frac{21}{3} = 7$		B0	

	23	B1		
11(b)	uidance			
	Embedded answer only of $23 - 11 = 12$			B0

11(c)	$\pm 2w \text{ or } \pm 18$ or $5w - 3w = 15 + 3$	Terms in w or constant terms	s collected	
	$2w = 18 \text{ or } -2w = -18 \text{ or } \frac{18}{2}$	A1		
	9 A1ft ft on $2w = a$ where $a \neq 3$ or or $bw = 18$ where $b \neq 5$ or 3			5
	Ad			
	2w = 12 6	M1 A0 A1ft		
	8w = 18 2.25 or $\frac{18}{8}$ oe			M1 A0 A1ft
	3w = 12 4			MO
	3w = 18			M1 A0 A0ft
	Embedded answer of 9			M1 A1 A0
	If only decimal answer given must be a	at least 2 dp		

Q	Answer		Mark	Comme	nts
	2, 3, 4, 6, 7, 8			B2 Six numbers, median Allow one of decimals or repeated numbers	s, numbers < 2
			B3	2, 2, 2, 8, 8, 8 or 2, 2.5, 4, 6, 7.5, 8 or 1, 2, 4, 6, 7, 10	
				B1 Any six numbers with	
				Allow cards to be in any order	
		Add	litional G	Buidance	
	Combinations for B2 that have repeats				
12	2, 2, 2, 8, 8, 8			2, 4, 4, 6, 6, 8	
	2, 2, 3, 7, 7, 9	2, 3, 3, 7, 7, 8	8	2, 4, 4, 6, 7, 7	
	2, 2, 3, 7, 8, 8	2, 3, 4, 6, 6, 9	9	2, 4, 5, 5, 5, 9	
	2, 2, 4, 6, 6, 10	2, 3, 5, 5, 5, ⁻	10	2, 4, 5, 5, 6, 8	
	2, 2, 4, 6, 7, 9	2, 3, 5, 5, 6, 9	9	2, 4, 5, 5, 7, 7	B2
	2, 2, 4, 6, 8, 8	2, 3, 5, 5, 7, 8	3		
	2, 2, 5, 5, 5, 11			2, 5, 5, 5, 5, 8	
	2, 2, 5, 5, 6, 10			2, 5, 5, 5, 6, 7	
	2, 2, 5, 5, 7, 9				
	2, 2, 5, 5, 8, 8				
	If answer line blank, mark working and apply usual rules for choice				

Q	Answer	Mark	Comn	nents
	1 – (0.2 + 0.3 + 0.15) or 0.65	M1	oe eg 65%	
	0.35	A1	oe eg 35%	
		Additional G	uidance	
	0.2 + 0.3 + 0.15 = 0.2 0.8	Answer follows thr	ough M1 A0	
13	0.2 + 0.3 + 0.15 = 0.55 1 - 0.55 = 0.25	Method even thou answer wrong	gh M1 A0	
	0.2 + 0.3 + 0.15 = 0.55 0.35	No method seen a answer does not fo through		
	0.65 0.45		M1 A0	
	Answer only of 0.65		M1 A0	
	0.2 0.8	No addition seen	MO	
	Embedded answer 0.2 + 0.3 + 0.15	Embedded answer 0.2 + 0.3 + 0.15 + 0.35 = 1		
	0.2 + 0.3 + 0.15 + 0.8 = 1 Answer 0.8		M1 A0	

Q	Answer	Mark	Comments		
	Side of square = 5		May be on diagram		
	or	B1			
	5 × 5 = 25 oe				
	400 ÷ 25	M1			
	16	A1	May be on diagram		
			16 $ imes$ 25 = 400 oe is M1 A1		
14	Yes and 5 and their 16	Q1ft	Strand (iii) Conclusion must b length not volume	e based on	
			ft their 16 if B1 M1 awarded a conclusion	and correct	
	Additional Guidance				
	Ignore any volume calculations				
	Square = 5 cm			B1	
	25 × 21 = 400			M1 A0	
	No			Q1ft	

15(a)	Café	B1	
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	[336, 340]	B2	B1 for [334, 342] but not [336, 340] which s or for [156, 160]	scores B2
	Ad			
15(b)	340			B2
15(b)	335			B1
	342			B1
	157			B1
	Ignore extra compass directions eg 338	3 NW		B2

Q	Answer	Mark	Comments	
Q 15(c)	Answer Point within tolerance (on bold line) Image: Constraint of the second s	Mark B2	Comments B1 Point [4, 5] squares on the line North of the Toilets or Point between 'rays'	
	Ad	ditional G	Toilets	
	Mark intention (point should be [0.2, 0.6	are down from top grid line)		
	Correct bearing drawn that stops at bol	Correct bearing drawn that stops at bold line		
	Correct bearing drawn that stops inside	e park	B1	

Q	Answer	Mark	Comments		
			·		
	Alternative method 1	1			
	<i>BCD</i> = 105	B1			
	<i>DCE</i> = 180 – their 105 or 75	M1	Calculation must be shown of marked on diagram	or correct angle	
	<i>CDE</i> = 180 – (their 75 + 30) or 75	M1dep	Calculation must be shown or correct a marked on diagram		
	DCE = 75 and $CDE = 75$ and 'two angles equal'	Q1	Strand (ii) Must score B1M2 and have no incorrect angles or calculations seen		
16	Additional Guidance				
	C = 105 C = 180 - 105 = 65 D = 180 - (65 + 30) = 85			B1 M1 M1dep Q0	
	BCD = 75 DCE = 180 - 75 = 105 CDE = 180 - (105 + 30) = 45			B0 M1 M1dep Q0	
	BCD = 105 DCE = 65 CDE = 85 (no method shown)			B1 M0 M0dep Q0	

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Q	Answer	Mark	Comments			
	Alternative method 2					
	<i>ABC</i> = 180 – 105 or 75 or <i>ADC</i> = 180 – 105 or 75	M1	Calculation must be shown or correct angle marked on diagram			
	DCE = their 75	M1dep	their 75 must be the same as their <i>ABC</i> or their <i>ADC</i>			
	<i>CDE</i> = 180 – (their 75 + 30) or 75	M1dep	Calculation must be shown or correct angle marked on diagram			
	DCE = 75 and CDE = 75 and 'two angles equal'	Q1	Strand (ii) Must score M3 and have no incorrect angles or calculations seen			
16 cont	Additional Guidance					
	B = 180 - 105 = 75 C = 105 D = 180 - (105 + 30) = 45		M1 M0dep M0dep Q0			
	ABC (or ADC) = 180 - 105 = 65 DCE = 65 CDE = 85 (no method shown)		M1 M1dep M0dep Q0			
	ABC (or ADC) = 180 - 105 = 75 DCE = 75 CDE = 180 - (75 + 30) = 65		M1 M1dep M1dep Q0			

Q	Answer	Mark	Comments	
	Alternative method 3			
	<i>BCD</i> = 105	B1		
	<i>CDE</i> = their 105 – 30 or 75	M1	Calculation must be shown or correct angle marked on diagram	
	DCE = 180 – (their 75 + 30) or 75	M1dep	Calculation must be shown or correct angle marked on diagram	
	DCE = 75 and CDE = 75 and 'two angles equal'	Q1	Strand (ii) Must score B1M2 and have no incorrect angles or calculations seen	
16 cont	Additional Guidance			
	C = 105 D = 105 - 30 = 65 C = 180 - (65 + 30) = 85		B1 M1 M1dep Q0	
	BCD = 75 CDE = 75 - 30 = 45 DCE = 180 - (45 + 30) = 105		B0 M1 M1dep Q0	
	BCD = 105 CDE = 65 DCE = 85 (no method shown)		B1 M0 M0dep Q0	

Q	Answer	Mark	Comments			
	Alternative method 4					
	<i>DCE</i> or <i>CDE</i> = (180 – 30) ÷ 2 or 75	M1	Calculation must be shown or o angle marked on diagram	one correct		
	CDE and DCE = their 75	M1dep				
	<i>DCB</i> = 180 – their 75 or 105 or <i>ABC</i> = their 75 or <i>ADC</i> = their 75	M1dep	Calculation must be shown or correct angl marked on diagram			
	<i>DCE</i> = 75 and <i>CDE</i> = 75 and <i>DCB</i> = 105 and 'opposite angles of parallelogram equal'		Strand (ii) Must score M3 and have no incorrect angles or calculations seen			
16 cont	or <i>DCE</i> = 75 and <i>CDE</i> = 75 and <i>ABC</i> or <i>ADC</i> = 75 and 'allied or (co)interior angles of parallelogram'	Q1				
	Additional Guidance					
	$(180 - 30) \div 2 = 65$ C = 65 and $D = 65C = 115$ (no method shown)		י ז	VI1 VI1dep VI0dep Q0		
	$(180 - 30) \div 2 = 75$ DCE = 75 and $CDE = 75DCB = 180 - 75 = 105$		r r	M1 M1dep M1dep Q0		

Q	Answer	Mark	Comments	
	•			
	2 × (30 + 70) or 200	M1		
	their 200 ÷ 4 or 50	M1dep	100 ÷ 2 is M2	
	their 50 \times their 50 or 2500 or 30 \times 70 or 2100	M1	their 50 must follow M1 M1dep	
	400	A1		
	Ac	Iditional G	buidance	
17	Perimeter = 100 Side of square = 25 2100 - 625 1475		M0 M0dep M1 A0	
	Side of square = $\sqrt{100}$ = 10 2100 - 100 2000		M0 M0dep M1 A0	
	$30 \times 70 = 2400$ $50 \times 50 = 2500$ 2500 - 2400 = 100		M1 M1dep M1 A0	
	Side of square = 25 $30 \times 70 = 2400$ Answer 625		M0 M0dep M1 A0	
	$30 \times 70 = 2100$ $2100 \times 2 = 4200$		3rd M0	

Q	Answer	Mark	Comments	
	Any correct product, or division with answer of 210 that involves a prime number eg $2 \times 105, 5 \times 42, 210 \div 3 = 70,$ $21 \times 2 \times 5$ or 2, 3, 5, 7	M1		
18	$2 \times 3 \times 5 \times 7$	A1		
	Additional Guidance			
	Product may be implied for M1 by a pri values written as pairs eg (2, 105)	M1		
	$1 \times 2 \times 3 \times 5 \times 7$			M1 A0

19	6 <i>n</i> + 3 or 3(2 <i>n</i> + 1)	B2	oe B1 for $6n$ Accept $6 \times n$ or $n \times 6$ but not $n6$ B1 for $n6 + 3$ Accept any letter
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20	360 ÷ 10 or 36 or 180 × (10 – 2) or 10 × 180 – 360 or 1440	M1	oe	
	144	A1		
	Ad	ditional	Guidance	
	Answer only of 144			M1 A1